

TABLE 11-1 COMPARISONS OF VELOCITY, IMPEDANCE, AND THE PROPAGATION CONSTANT FOR FREE SPACE, LOSSLESS MATERIAL, AND CONDUCTING OR LOSSY MATERIAL

	Velocity	Intrinsic impedance	Propagation constant
Free space	$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} = \frac{\omega}{\beta}$ $\approx 3 \times 10^8 \text{ (m s}^{-1}\text{)}$	$\eta = \sqrt{\frac{\mu_0}{\epsilon_0}} \approx 120\pi \text{ } (\Omega)$ $\approx 377\Omega$	$\gamma = j\beta$ $= j\omega\sqrt{\mu_0\epsilon_0} \text{ (m}^{-1}\text{)}$
Lossless dielectric	$U = \frac{1}{\sqrt{\mu\epsilon}} = \frac{c}{\sqrt{\mu_r\epsilon_r}}$ $= \frac{\omega}{\beta} \text{ (m s}^{-1}\text{)}$	$\eta = \sqrt{\frac{\mu}{\epsilon}} = \sqrt{\frac{\mu_0\mu_r}{\epsilon_0\epsilon_r}}$ $\approx 120\pi\sqrt{\frac{\mu_r}{\epsilon_r}} \text{ } (\Omega)$	$\gamma = j\beta$ $= j\omega\sqrt{\mu_0\epsilon_0\mu_r\epsilon_r} \text{ (m}^{-1}\text{)}$
Lossy dielectric, $\epsilon = \epsilon' - j\frac{\sigma}{\omega}$	$U = \frac{\omega}{\beta} \text{ (m s}^{-1}\text{)}$	$\eta = \frac{\sqrt{\mu/\epsilon'}}{\sqrt{1 - j\frac{\sigma}{\omega\epsilon'}}} \text{ } (\Omega)$	$\gamma = \alpha + j\beta$ $= j\omega\sqrt{\mu\epsilon'} \left(\sqrt{1 - j\frac{\sigma}{\omega\epsilon'}} \right) \text{ (m}^{-1}\text{)}$
Slightly lossy dielectric, $\frac{\sigma}{\omega\epsilon'} \ll 1$	$U = \frac{\omega}{\beta} \text{ (m s}^{-1}\text{)}$	$\eta \approx \sqrt{\frac{\mu}{\epsilon'}} \left(1 + j\frac{\sigma}{2\omega\epsilon'} \right) \text{ } (\Omega)$	$\gamma = \alpha + j\beta$ $\approx j\omega\sqrt{\mu\epsilon'} \left(1 - j\frac{\sigma}{2\omega\epsilon'} \right) \text{ (m}^{-1}\text{)}$
Good conductor $\frac{\sigma}{\omega\epsilon'} \gg 1$	$U = \frac{\omega}{\beta} \text{ (m s}^{-1}\text{)}$	$\eta \approx \sqrt{\frac{\omega\mu}{\sigma}} \angle 45^\circ \text{ } (\Omega)$	$\gamma = \alpha + j\beta$ $\approx \sqrt{\pi f\mu\sigma} (1 + j) \text{ (m}^{-1}\text{)}$